

$$c = \frac{a + b}{2} \tag{1a}$$

Ako je $f(a)f(c) < 0$: $a = a, b = c$ (1b)

Ako je $f(c)f(b) < 0$: $a = c, b = b$ (1c)

Ako je $f(a)f(c) = 0$: dobiva se rješenje $\xi = c$ (1d)

$$|b - a| \leq \varepsilon_1 \quad \text{i/ili} \quad |f(x_i)| \leq \varepsilon_2 \tag{2}$$

$$x_i = b - \frac{b - a}{f(b) - f(a)} f(b) \tag{3a}$$

Ako je $f(a)f(x_i) < 0$: $a = a, b = x_i$ (3b)

Ako je $f(x_i)f(b) < 0$: $a = x_i, b = b$ (3c)

Ako je $f(a)f(x_i) = 0$: dobiva se rješenje $\xi = x_i$ (3d)

$$|b - a| \leq \varepsilon_1 \quad \text{i/ili} \quad |f(x_i)| \leq \varepsilon_2 \tag{4}$$

$$x_{i+1} = g(x_i) \tag{5}$$

$$|x_{i+1} - x_i| \leq \varepsilon_1 \quad \text{i/ili} \quad |f(x_{i+1})| \leq \varepsilon_2 \tag{6}$$

$$\left| \frac{e_{i+1}}{e_i} \right| = |g'(\zeta)| < 1 \tag{7}$$

$$x_{i+1} = x_i - \frac{f(x_i)}{f'(x_i)} \tag{8}$$

$$|x_{i+1} - x_i| \leq \varepsilon_1 \quad \text{i/ili} \quad |f(x_{i+1})| \leq \varepsilon_2 \tag{9}$$

$$x_{i+1} = x_i - \frac{f(x_i)}{f'(x_0)} \tag{10}$$

$$x_{i+1} = x_i - \frac{x_i - x_{i-1}}{f(x_i) - f(x_{i-1})} f(x_i) \tag{11}$$

$$\mathbf{Ax} = \mathbf{b} \tag{12}$$

$$\sum_{j=1}^n a_{ij} x_j = b_i \quad (i = 1, 2, \dots, n) \tag{13}$$

$$[\mathbf{A}|\mathbf{I}] \rightarrow [\mathbf{I}|\mathbf{A}^{-1}] \tag{14}$$

$$\mathbf{x} = \mathbf{A}^{-1}\mathbf{b} \tag{15}$$

$$\mathbf{A} = \mathbf{L}\mathbf{U} \tag{16}$$

$$\mathbf{L}\mathbf{b}' = \mathbf{b} \Rightarrow \mathbf{b}' \tag{17}$$

$$\mathbf{U}\mathbf{x} = \mathbf{b}' \Rightarrow \mathbf{x} \tag{18}$$

$$x_i^{(k+1)} = x_i^{(k)} + \frac{1}{a_{ii}} \left(b_i - \sum_{j=1}^n a_{ij}x_j^{(k)} \right) \quad (i = 1, 2, \dots, n) \tag{19}$$

$$x_i^{(k+1)} = x_i^{(k)} + \frac{R_i^{(k)}}{a_{ii}} \quad (i = 1, 2, \dots, n) \tag{20}$$

$$R_i^{(k)} = b_i - \sum_{j=1}^n a_{ij}x_j^{(k)} \quad (i = 1, 2, \dots, n) \tag{21}$$

$$x_i^{(k+1)} = x_i^{(k)} + \frac{R_i^{(k)}}{a_{ii}} \quad (i = 1, 2, \dots, n) \tag{22}$$

$$R_i^{(k)} = b_i - \sum_{j=1}^{i-1} a_{ij}x_j^{(k+1)} - \sum_{j=i}^n a_{ij}x_j^{(k)} \quad (i = 1, 2, \dots, n) \tag{23}$$

$$x_i^{(k+1)} = x_i^{(k)} + \omega \frac{R_i^{(k)}}{a_{ii}} \quad (i = 1, 2, \dots, n) \tag{24}$$

$$R_i^{(k)} = b_i - \sum_{j=1}^{i-1} a_{ij}x_j^{(k+1)} - \sum_{j=i}^n a_{ij}x_j^{(k)} \quad (i = 1, 2, \dots, n) \tag{25}$$

$$P_n(x) = a_0 + a_1x + a_2x^2 + \dots + a_nx^n \tag{26}$$

$$\begin{aligned} y_0 &= a_0 + a_1x_0 + a_2x_0^2 + \dots + a_nx_0^n \\ y_1 &= a_0 + a_1x_1 + a_2x_1^2 + \dots + a_nx_1^n \\ y_2 &= a_0 + a_1x_2 + a_2x_2^2 + \dots + a_nx_2^n \\ &\dots\dots\dots \\ y_n &= a_0 + a_1x_n + a_2x_n^2 + \dots + a_nx_n^n \end{aligned} \tag{27}$$

$$P_n(x) = \sum_{k=0}^n L_k(x)f(x_k) \tag{28}$$

$$L_k(x) = \frac{(x - x_0) \dots (x - x_{k-1})(x - x_{k+1}) \dots (x - x_n)}{(x_k - x_0) \dots (x_k - x_{k-1})(x_k - x_{k+1}) \dots (x_k - x_n)}$$

$$= \prod_{\substack{i=0 \\ i \neq k}}^n \frac{x - x_i}{x_k - x_i} \quad (k = 0, 1, \dots, n)$$
(29)

$$P_n(x) = f_0 + \binom{s}{1} \Delta f_0 + \binom{s}{2} \Delta^2 f_0 + \dots + \binom{s}{n} \Delta^n f_0$$
(30)

$$s = \frac{x - x_0}{h} \quad \text{pa je} \quad x = x_0 + sh$$
(31)

$$h = x_i - x_{i-1}$$
(32)

$$\Delta f_0 = f_1 - f_0$$

$$\Delta^2 f_0 = \Delta f_1 - \Delta f_0 = f_2 - 2f_1 + f_0$$

.....

$$\Delta^n f_0 = \Delta^{n-1} f_1 - \Delta^{n-1} f_0 = \sum_{i=0}^n (-1)^i \binom{n}{i} f_i$$
(33)

$$P_n(x) = f_0 + \binom{s^+}{1} \Delta f_0 + \binom{s^+}{2} \Delta^2 f_0 + \dots + \binom{s^+}{n} \Delta^n f_0$$
(34)

$$\binom{s^+}{i} = \frac{s(s+1)(s+2) \dots (s+[i-1])}{i!}$$
(35)

$$y = a_0 + a_1x + a_2x^2 + \dots + a_nx^n$$
(36)

$$\frac{\partial S}{\partial a_k} = \sum_{i=1}^N 2(Y_i - a_0 - a_1x_i - \dots - a_nx_i^n)(-x_i^k) = 0 \quad (k = 0, 1, \dots, n)$$
(37)

$$a_0N + a_1 \sum_{i=1}^N x_i + \dots + a_n \sum_{i=1}^N x_i^n = \sum_{i=1}^N Y_i$$

.....

(38)

$$a_0 \sum_{i=1}^N x_i^n + a_1 \sum_{i=1}^N x_i^{n+1} + \dots + a_n \sum_{i=1}^N x_i^{2n} = \sum_{i=1}^N x_i^n Y_i$$

$$y = ax^b$$
(39)

$$\ln(y) = \ln a + b \ln(x)$$
(40)

$$Y = \ln(y) \quad A = \ln(a) \quad X = \ln(x) \quad iB = b$$
(41)

$$Y = A + Bx$$
(42)

$$y = ae^{bx}$$
(43)

$$\ln(y) = \ln a + bx \Rightarrow Y = A + bx$$
(44)

$$P_n(x) = a_0 + a_1x + a_2x^2 + \dots + a_nx^n \quad (45)$$

$$f'(x) \cong P'(x) = a_1 + 2a_2x + 3a_3x^2 + \dots + na_nx^{n-1} \quad (46)$$

$$f''(x) \cong P''(x) = 2a_2 + 6a_3x + \dots + n(n-1)a_nx^{n-2} \quad (47)$$

$$f'(x_i) \approx \frac{f(x_i+h) - f(x_i)}{h} \quad (48)$$

$$f'(x_i) \approx \frac{f(x_i) - f(x_i-h)}{h} \quad (49)$$

$$f'(x_i) \approx \frac{f(x_i+h) - f(x_i-h)}{2h} \quad (50)$$

$$f(x) \approx P_n(x) = a_0 + a_1x + a_2x^2 + \dots \quad (51)$$

$$I = \int_a^b f(x)dx \approx \int_a^b P_n(x)dx = \left(a_0x + a_1\frac{x^2}{2} + \dots \right) \Big|_a^b \quad (52)$$

$$I = \int_a^b f(x)dx \approx \frac{b-a}{n} \left[\frac{1}{2}(f_0 + f_n) + \sum_{j=1}^{n-1} f_j \right] \quad (53)$$

$$I = \int_a^b f(x)dx \approx \frac{b-a}{6n} \left[f_0 + f_{2n} + 4 \sum_{j=0}^{n-1} f_{2j+1} + 2 \sum_{j=1}^{n-1} f_{2j} \right] \quad (54)$$

$$\begin{aligned} I &= \int_a^b f(x)dx = \int_{-1}^1 f(mt+c)m dt = \frac{b-a}{2} \int_{-1}^1 F[t]dt \\ &= \frac{b-a}{2} \left(F\left(-\frac{1}{\sqrt{3}}\right) + F\left(\frac{1}{\sqrt{3}}\right) \right) \end{aligned} \quad (55)$$

$$m = \frac{b-a}{2} \quad \text{i} \quad c = \frac{b+a}{2} \quad (56)$$

$$y(t) = y(t_0) + y'(t_0)\Delta t + \frac{y''(t_0)}{2}(\Delta t)^2 + \dots + \frac{y^{(n)}(t_0)}{n!}(\Delta t)^n + \dots \quad (57)$$

$$y'' = \frac{\partial y'}{\partial t} + \frac{\partial y'}{\partial y} \frac{dy}{dt} = y'_t + y'_y y' \quad (58)$$

$$y''' = y'_{tt} + 2y'_{ty}y' + y'_t y'_y + (y'_y)^2 y' + y'_{yy} (y')^2 \quad (59)$$

$$y_{n+1} = y_n + h f(t_n, y_n) \quad (60)$$

$$y_{n+1} = y_n + h f(t_{n+1}, y_{n+1}) \quad (61)$$

$$y_{n+1} = y_n + \frac{1}{2}\Delta y_1 + \frac{1}{2}\Delta y_2 = y_n + \frac{h}{2}(f_n + f_{n+1}) \quad (62a)$$

$$\Delta y_1 = hf(t_n, y_n) = hf_n \quad (62b)$$

$$\Delta y_2 = hf(t_n + \Delta t, y_n + \Delta y_1) = hf_{n+1} \quad (62c)$$

$$y_{n+1} = y_n + 0 \cdot \Delta y_1 + 1 \cdot \Delta y_2 = y_n + hf_{n+1/2} \quad (63a)$$

$$\Delta y_1 = hf(t_n, y_n) = hf_n \quad (63b)$$

$$\Delta y_2 = hf\left(t_n + \frac{h}{2}, y_n + \frac{\Delta y_1}{2}\right) = hf_{n+1/2} \quad (63c)$$

$$y_{n+1} = y_n + \frac{1}{6}(\Delta y_1 + 2\Delta y_2 + 2\Delta y_3 + \Delta y_4) \quad (64)$$

$$\Delta y_1 = hf(t_n, y_n) \quad (65a)$$

$$\Delta y_2 = hf\left(t_n + \frac{h}{2}, y_n + \frac{\Delta y_1}{2}\right) \quad (65b)$$

$$\Delta y_3 = hf\left(t_n + \frac{h}{2}, y_n + \frac{\Delta y_2}{2}\right) \quad (65c)$$

$$\Delta y_4 = hf(t_n + h, y_n + \Delta y_3) \quad (65d)$$
